

[2] FIRST CURVE

$$\frac{d}{dx}(e^{-2x} \cos 2y + x^2 - y^2) = \frac{d}{dx}(1)$$

$$8 \quad -2e^{-2x} \cos 2y - 2e^{-2x} \sin 2y \frac{dy}{dx} + 2x - 2y \frac{dy}{dx} = 0$$

$$2 \quad x - e^{-2x} \cos 2y = (e^{-2x} \sin 2y + y) \frac{dy}{dx}$$

$$2 \quad \frac{dy}{dx} = \frac{x - e^{-2x} \cos 2y}{y + e^{-2x} \sin 2y}$$

SECOND CURVE

$$\frac{d}{dx}(e^{-2x} \sin 2y - 2xy) = \frac{d}{dx} 1$$

$$8 \quad -2e^{-2x} \sin 2y + 2e^{-2x} \cos 2y \frac{dy}{dx} - 2y - 2x \frac{dy}{dx} = 0$$

$$2 \quad (e^{-2x} \cos 2y - x) \frac{dy}{dx} = e^{-2x} \sin 2y + y$$

$$2 \quad \frac{dy}{dx} = \frac{e^{-2x} \sin 2y + y}{e^{-2x} \cos 2y - x}$$

$$= - \frac{1}{\frac{x - e^{-2x} \cos 2y}{y + e^{-2x} \sin 2y}}$$

8 SLOPES ARE NEGATIVE RECIPROCAL  
SO TANGENT LINES ARE PERPENDICULAR

$$[3] [a] \frac{d^3}{dx^3} \frac{\frac{1}{\cos x} - \sin x}{\frac{\sin x}{\cos x}} = \frac{d^3}{dx^3} \left( \frac{1}{\cos x} - \sin x \right) \cdot \frac{\cos x}{\sin x}$$

$$= \frac{d^3}{dx^3} (\csc x - \cos x)$$

4

$$= \frac{d^2}{dx^2} (-\csc x \cot x + \sin x)$$

4

$$= \frac{d}{dx} (\csc x \cot x \cot x - \csc x (-\csc^2 x) + \cos x)$$

6

$$= \frac{d}{dx} (\csc x \cot^2 x + \csc^3 x + \cos x)$$

2

$$= \left[ -\csc x \cot x \cot^2 x + \csc x (2 \cot x) (-\csc^2 x) + 3 \csc^2 x (-\csc x \cot x) - \sin x \right]$$

8

$$\left[ \begin{array}{l} -\csc x \cot^3 x \\ -5 \csc^3 x \cot x \\ -\sin x \end{array} \right]$$

4

$$[b] \quad y = \frac{(x^4 - 2x + 1)^{\frac{1}{3}} (\sec x)^4}{e^{x^2} \arcsin x}$$

$$8 \quad \ln y = \frac{1}{3} \ln(x^4 - 2x + 1) + 4 \ln(\sec x) - x^2 - \ln(\arcsin x)$$

$$2 \quad \frac{1}{y} \frac{dy}{dx} = \frac{1}{3} \frac{1}{x^4 - 2x + 1} (4x^3 - 2) + 4 \frac{1}{\sec x} \sec x \tan x - 2x$$

$$= \frac{4x^3 - 2}{3(x^4 - 2x + 1)} + 4 \tan x - 2x - \frac{1}{\sqrt{1-x^2} \arcsin x}$$

$$\frac{dy}{dx} = \frac{\sqrt[3]{1-2x+x^4} \sec^4 x}{e^{x^2} \sin^{-1} x} \left[ \frac{4x^3 - 2}{3(1-2x+x^4)} + 4 \tan x - 2x - \frac{1}{\sqrt{1-x^2} \sin^{-1} x} \right]$$

$$[4][a] f(x) = x^{-\frac{1}{3}} \rightarrow f'(x) = -\frac{1}{3} x^{-\frac{4}{3}}$$

$$f'(8) = -\frac{1}{3} (8)^{-\frac{4}{3}} = -\frac{1}{3} \frac{1}{(\sqrt[3]{8})^4} = -\frac{1}{3} \frac{1}{16}$$

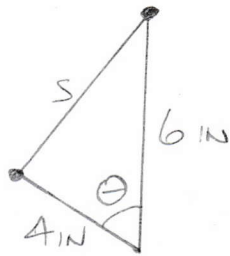
$$= -\frac{1}{48}$$

$$dy = -\frac{1}{48} (8.06 - 8) = -\frac{1}{48} \cdot \frac{6}{100} = -\frac{1}{800}$$

$$[b] y = 8^{-\frac{1}{3}} = \frac{1}{\sqrt[3]{8}} = \frac{1}{2}$$

$$\frac{1}{\sqrt[3]{8.06}} \approx \frac{1}{2} - \frac{1}{800} = \frac{399}{800}$$

[5]



$$\frac{d\theta}{dt} = \frac{-2\pi \text{ RADIANS}}{\text{HOUR}}$$

WANT  $\left. \frac{ds}{dt} \right|_{\theta = \frac{\pi}{3}}$

$$s^2 = (6 \text{ IN})^2 + (4 \text{ IN})^2 - 2(6 \text{ IN})(4 \text{ IN}) \cos \theta$$

$$= (52 - 48 \cos \theta) \text{ IN}^2 \quad \leftarrow \theta = \frac{\pi}{3}$$

$$2s \frac{ds}{dt} = (48 \sin \theta) \frac{d\theta}{dt} \text{ IN}^2$$

$$2(2\sqrt{7} \text{ IN}) \left. \frac{ds}{dt} \right|_{\theta = \frac{\pi}{3}} = 48 \cdot \frac{\sqrt{3}}{2} \cdot \frac{-2\pi \text{ RADIANS}}{\text{HR}} \text{ IN}^2$$

$$s = 2\sqrt{7} \text{ IN}$$

$$\left. \frac{ds}{dt} \right|_{\theta = \frac{\pi}{3}} = \frac{-12\sqrt{3}\pi}{\sqrt{7}} \frac{\text{IN}}{\text{HR}} = \frac{-12\sqrt{21}\pi}{7} \frac{\text{IN}}{\text{HR}}$$

THE TIP OF THE MINUTE HAND IS GETTING CLOSER TO THE CRYSTAL BY  $\frac{12\sqrt{21}\pi}{7}$  INCHES PER HOUR

OR  $\frac{\sqrt{21}\pi}{35}$  INCHES PER MINUTE AT 8:50 PM

$$[6] \quad x=5 \rightarrow y = \arctan \frac{m(5)}{2(5)-11} = \arctan \frac{1}{-1} = \arctan(-1) = -\frac{\pi}{4}$$

$$\frac{dy}{dx} = \left[ \frac{1}{1 + \left( \frac{m(x)}{2x-11} \right)^2} \right] \cdot \left[ \frac{m'(x)(2x-11) - m(x) \cdot 2}{(2x-11)^2} \right]$$

$$\left. \frac{dy}{dx} \right|_{x=5} = \left[ \frac{1}{1 + \left( \frac{1}{-1} \right)^2} \right] \cdot \left[ \frac{3(-1) - 1(2)}{(-1)^2} \right] = \frac{1}{2} \cdot \frac{-5}{1} = -\frac{5}{2}$$

$$\text{SLOPE OF NORMAL LINE} = -\frac{1}{-\frac{5}{2}} = \frac{2}{5}$$

$$y - -\frac{\pi}{4} = \frac{2}{5}(x-5)$$

$$y + \frac{\pi}{4} = \frac{2}{5}(x-5)$$